## Kinross High School



Maths and Numeracy Methodology Booklet A Guide for Teachers and Parents/Carers

## Introduction

Numeracy is a skill for life, learning and work. Having well-developed numeracy skills allows young people to be more confident in social settings and enhances enjoyment in a large number of leisure activities.

## What is the purpose of the booklet?

This booklet has been produced to give guidance to staff \& parents/carers on how certain common Numeracy topics are taught within the Mathematics department for problem solving, following the Curriculum for Excellence guidelines used in all schools in Scotland.

## Curriculum for Excellence Numeracy Strands

Number, Money and Measure<br>Estimation and Rounding<br>Number and number processes<br>Fractions, Decimals and Percentages<br>Money<br>Time<br>Measurement<br>Data and Analysis<br>Ideas of chance and uncertainty

## How can it be used?

Before teaching a topic containing numeracy you can refer to the booklet to see what methods are being taught.
A timeline of when topics are taught in S1/S2 is included at the end of this booklet.

Why do some topics include more than one method?
In some cases (e.g. percentages), the method used will be dependent on the level of difficulty of the question, and whether or not a calculator is permitted.

For mental calculations, pupils should be encouraged to develop a variety of strategies so that they can select the most appropriate method in any given situation.

For calculator questions do try to estimate the answer mentally first.

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## Addition

## Mental Strategies

There are a number of useful mental strategies for addition. Some examples are given below.

Example Calculate 64+27
Method 1 Add tens, then units, then add together

$$
60+20=80 \quad 4+7=11 \quad 80+11=91
$$

Method 2 Split up number to be added (last number 27) into tens and units and add separately.

$$
64+20=84 \quad 84+7=91
$$

Method 3 Round up to nearest 10, then subtract. $64+30=94$ but 30 is 3 too much so subtract 3 ;
$94-3=91$

## Written Method

When adding numbers, ensure that the numbers are lined up according to place value. Start at right hand side, write down units, carry tens.

Example Add 3032 and 589



## Subtraction



We use decomposition as a written method for subtraction (see below). Alternative methods may be used for mental calculations

## Mental Strategies

Example 1 Calculate 93-56

## Method 1 Count on

Count on from 56 until you reach 93 . This can be done in several ways.


Method 2 Break up the number being subtracted
E.g. subtract 50 , then subtract 6 .


## Written Method

Example 1 4590-386 $459{ }^{8} 0$ - 386 4204

Example 2 Subtract 692 from 14597 14597 - 692

13905

Important steps for example 1

1. Say "zero subtract 6 , we can't do this"
2. Look to next column exchange one ten for ten units, ie 9 tens becomes 8 \& 10 units
3. Then say "ten take away six equals four"
4. Normal subtraction rules can be used to then complete the question.

## Multiplication 1

It is essential that you know all of the multiplication tables from 1 to 10. These are shown in the tables square below.

| $\times$ | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | :---: |
| 1 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| 2 | 2 | 4 | 6 | 8 | 10 | 12 | 14 | 16 | 18 | 20 |
| 3 | 3 | 6 | 9 | 12 | 15 | 18 | 21 | 24 | 27 | 30 |
| 4 | 4 | 8 | 12 | 16 | 20 | 24 | 28 | 32 | 36 | 40 |
| 5 | 5 | 10 | 15 | 20 | 25 | 30 | 35 | 40 | 45 | 50 |
| 6 | 6 | 12 | 18 | 24 | 30 | 36 | 42 | 48 | 54 | 60 |
| 7 | 7 | 14 | 21 | 28 | 35 | 42 | 49 | 56 | 63 | 70 |
| 8 | 8 | 16 | 24 | 32 | 40 | 48 | 56 | 64 | 72 | 80 |
| 9 | 9 | 18 | 27 | 36 | 45 | 54 | 63 | 72 | 81 | 90 |
| 10 | 10 | 20 | 30 | 40 | 50 | 60 | 70 | 80 | 90 | 100 |

## Mental Strategies

Example Find $39 \times 6$

## Method 1



Method 2


## Multiplication 2



When using written methods for multiplication, we use the Grid Method to answer questions. Break numbers up into "easy" numbers that add to give that number, then multiply. Once you have multiplied, add up all your answers!

Example 1 a) Multiply 39 by 6:


| $X$ | 30 | 9 |
| :--- | :--- | :--- |
| 6 | 180 | 54 |

b) Multiply 156 by 62


| $X$ | 100 | 50 | 6 |
| :--- | :--- | :--- | :--- |
| 60 | 6000 | 3000 | 360 |
| 2 | 200 | 100 | 12 |

Then sum these answers:

$$
\begin{aligned}
39 \times 6= & 180+54 \\
& =234
\end{aligned}
$$

$156 \times 62=6000+3000+360$

$$
+200+100+12
$$

$=9672$

We can also use this method when multiplying decimals
Example 2: Find $2.36 \times 38.4$

| $X$ | 2 | 0.3 | 0.06 |
| :---: | :---: | :---: | :---: |
| 30 | 60 | 9 | 1.8 |
| 8 | 16 | 2.4 | 0.48 |
| 0.4 | 0.8 | 0.12 | 0.024 |
|  | $2.36 \times 38.4=$ | $60+9+1.8+16$ |  |
|  |  |  |  |
|  | $+2.4+0.48+0.8$ |  |  |
|  | $+0.12+0.024$ |  |  |
|  | $=90.624$ |  |  |

## Division



## Written Method

Example 1 There are 192 pupils in first year, shared equally between 8 classes. How many pupils are in each class?
$8 \quad \frac{24}{19^{13} 2} \quad$ There are 24 pupils in each class
Example 2 Divide 4.74 by 3

$$
3 \longdiv { 1 . 5 8 } \begin{array} { | c } 
{ 4 . 7 ^ { 2 } 4 }
\end{array}
$$

When dividing a decimal number by a whole number, the decimal points must stay in line.

Example 3 A jug contains 2.2 litres of juice. If it is poured evenly into 8 glasses, how much juice is in each glass?
$8 \quad \begin{aligned} & 0.275 \\ & 2^{6} 0^{4} 0\end{aligned}$

Each glass contains 0.275 litres
If you have a remainder at the end of a calculation, add a zero onto the end of the decimal and continue with the calculation.

Long Division - This is not a feature in modern day courses although we do show our more able pupils. In general, we would expect Pupils to estimate the answer and then use a calculator to get the exact answer.

## Order of Calculations (BODMAS/ BIDMAS)

Consider this: what is the correct answer to $2+4 \times 5$ ?
Is it

$$
\begin{array}{lll}
(2+4) \times 5 & \text { OR } & 2+(4 \times 5) \\
=6 \times 5 & & =2+20 \\
=30 & & =22
\end{array}
$$

The correct answer is 22 .

The mnemonic tells us which operation should be done first.
BODMAS (BIDMAS) represents: (B)rackets
(O/I)rder or (I)ndices
(D)ivision
(M)ultiply
(A)dd
(S)ubtract

Therefore in the example above multiplication should be done before addition.
Note: 'order' means a number raised ro a power such as $2^{2}$ or $(-3)^{4}$.
Scientific calculators are programmed with these rules, however some basic calculators may not so take care.

Example $1 \quad 15-12 \div 6 \quad$ BODMAS tells us to divide first

$$
\begin{aligned}
& =15-2 \\
& =13
\end{aligned}
$$

Example $2(9+5) \times 6$
BODMAS tells us to work out the

$$
\begin{aligned}
& =14 \times 6 \\
& =84
\end{aligned}
$$

Example $3 \quad 18+6 \div(5-2) \quad$ Brackets first

$$
\begin{array}{ll}
=18+6 \div 3 & \\
\text { Then divide } \\
=18+2 & \\
\text { Now add }
\end{array}
$$

$$
=20
$$

Example 4
Add \& subtract have equal priority
$=12+2$ So subtract
$=14$
Now add

12- Hour clock Time can be displayed on a clock face, or digital clock


05: 15
These clocks both show fifteen minutes past five, or quarter past five.

When writing in 12 hour clock we need to add a.m or p.m. after the time. a.m. is used for times between midnight and 12 noon (morning).
p.m. is used for times between 12 noon and midnight (afternoon/ evening).

## 24- Hour clock



In 24 hour clock, the hours are written as number between 00 and 24. Midnight is expressed as 0000. After 12 noon, the hours are numbered $13,14,15 \ldots$ etc


Reading timetables
When reading timetables you often have to convert to and from 24 hours clock.
To convert from 24 hour time to 12 hour time:
If the hour is 13 or more, subtract 12 from the hours and call it P.M. Otherwise it is A.M.

If the hour is 12 , leave it unchanged, but call it P.M.
If the hour is 0 , make it 12 and call it A.M.
Otherwise, leave the hour unchanged and call it A.M.
To convert from 12-hour time to 24-hour time:
If the P.M. hour is from 1 through 11, add 12.
If the P.M. hour is 12 , leave it as is.
If the A.M. hour is 12 , make it 0 .
Otherwise, leave the hour unchanged. Then drop the A.M. or P.M., of course.

## Time 2

## Time Facts

It is essential to know the number of months, weeks and days in a year, and the number of days in each month.

Time Calculations

Example 1 How long is it from 0755 to 0948 ?

Method-Working (use a time line)

| 0755 | -> 0800 | $\rightarrow$ | 0900 | $\rightarrow>$ |
| :---: | :---: | :---: | :---: | :---: |
| (5mins) | ( 1 hr ) | (48mins) |  |  |

Then add total time to give 1 hr 53 mins

## ***WE DON'T TEACH TIME AS SUBTRACTION***

Example 2 Change 27 minutes into decimals hours

27 mins $=27 \div 60=0.45$ Hours


Addition, subtraction, multiplication and division of fractions are studied in mathematics. However, the examples below may be helpful in all subjects

## Understanding Fractions

## Example

A jar contains black and white sweets.
What fractions of the sweets are black?


There are 3 black sweets out of total of 7 , so $\frac{3}{8}$ of the sweets are black.
NOTE: Please encourage pupils to write fractions as above and not at $3 / 8$. It is important that pupils recognise the different parts of the fraction.

## Equivalent Fractions

## Example

What fraction of the flag is shaded?


6 out of the 12 are shaded. So $\frac{6}{12}$ of the flag is shaded.
It could also be said that $\frac{1}{2}$ of the flag is shaded and that $\frac{6}{12}$ and $\frac{1}{2}$ are equivalent
fractions.

## Fractions 2

## Simplifying Fractions



The top of a fraction is called the numerator: the bottom is called the denominator.
To simplify a fraction, divide the numerator and denominator of the fraction by the same number.

## Example 1

(a)

(b)


This can be done repeatedly until the numerator and denominator are the smallest possible number-the fraction is then said to be in it simplest form.

Example 2 Simplify $\frac{72}{84} \quad \frac{72}{84}=\frac{36}{42}=\frac{18}{21}=\frac{6}{7}$ (Simplest form)

## Calculating Fractions of a Quantity



To find the fraction of a quantity, divide by the denominator.
To find $\frac{1}{2}$ divide by 2 , to find $\frac{1}{4}$ divide by 4 , to find $\frac{1}{8}$ divide by 8 etc. If the fraction has a numerator not equal to 1 we then need to multiply our answer by the numerator.

Example 1 Find $\frac{1}{5}$ of $£ 150$

$$
\frac{1}{5} \text { of } £ 150=£ 150 \div 5=£ 30
$$

Example 2 Find $\frac{3}{4}$ of 48

$$
\begin{aligned}
& \frac{1}{4} \text { of } 48=48 \div 4=12 \\
& \text { so } \frac{3}{4} \text { of } 48=3 \times 12=36
\end{aligned}
$$

To find $\frac{3}{4}$ of a quantity, start by finding $\frac{1}{4}$ then multiply by 3 (the numerator)

## Percentages 1

Percent means out of 100. A percentage can be converted to an equivalent fraction or decimal.
$36 \%$ means $\frac{36}{100}$
$36 \%$ is therefore equivalent to $\frac{9}{25}$ and 0.36

To change a fraction to a decimal (fraction) divide the numerator by the denominator.

## Common Percentages

Some percentages are used very frequently. It is useful to know these as fractions and decimals.

| Percentage | Fraction | Decimal (Fraction) |
| :---: | :---: | :---: |
| $1 \%$ | $\frac{1}{100}$ | 0.01 |
| $10 \%$ | $\frac{1}{10}$ | 0.1 |
| $20 \%$ | $\frac{1}{5}$ | 0.2 |
| $25 \%$ | $\frac{1}{4}$ | 0.25 |
| $33^{1 / 3 \%}$ | $\frac{1}{3}$ | $0.333 \ldots$ |
| $50 \%$ | $\frac{1}{2}$ | 0.5 |
| $66^{2} / 3 \%$ | $\frac{2}{3}$ | $0.666 \ldots$ |
| $75 \%$ | $\frac{3}{4}$ | 0.75 |

## Percentages 2

There are many ways to calculate percentages of a quantity. Some of the common ways are shown below.

## Non-Calculator Methods

## Method 1: Using Equivalent Fractions

In this method, we replace our percentage with an equivalent common fraction we can easily find, then multiply to give the required value.

Example 1 Find $9 \%$ of 200 g
$1 \%$ of $200 \mathrm{~g}=\frac{1}{100}$ of $200 \mathrm{~g}=200 \mathrm{~g} \div 100=2 g$
So $9 \%$ of $200 g=9 \times 2 g=18 g$

Example 2 Find 70\% of $£ 35$
$10 \%$ of $£ 35=\frac{1}{10}$ of $£ 35=£ 35 \div 10=£ 3.50$
So $70 \%$ of $£ 35=7 \times £ 3.50=£ 24.50$

## Method 2: Using a Combination of Equivalent Fractions

The previous examples can be used in combinations as to calculate any percentage.
We can "break apart" our percentages into multiples of $10 \%$ and $1 \%$

Example 3 Find $23 \%$ of $£ 15000$
$23 \%$ can be broken up into $20 \%$ and $3 \%$.
$10 \%$ of $£ 15000=£ 1500$ so $20 \%=£ 1500 \times 2=£ 3000$
$1 \%$ of $£ 15000=£ 150$ so $3 \%=£ 150 \times 3=£ 450$
$23 \%$ of $£ 15000=£ 3000+£ 450=£ 3450$.

## Percentages 3

## Calculator Methods

To find a percentage of a quantity using a calculator, change the percentage to a decimal by dividing by 100 and then multiply.

To find a percentage of a total, first make a fraction, then convert to a decimal by dividing the top by the bottom. This can then be expressed as a percentage by multiplying by 100.

Example 1 There are 30 pupils in Class 3A3. 18 are girls. What percentage of Class 3A3 are girls?

$$
\frac{18}{30}=18 \div 30=0.6=60 \%
$$

So $60 \%$ of 3 A3 are girls.

Example 2 James scored 36 out of 44 in his biology test.
What is his percentage mark?

$$
\text { Score }=\frac{36}{44}=36 \div 44=0.81818 \ldots
$$

$$
=81.818 \ldots \%=82 \% \text { (rounded) }
$$

## Percentages 4

## Percentages Changes



## Example 1: Percentage Increase/Decrease

Increase $£ 300$ by $24 \%$

Using the methods previously spoke about 24\% can be broken up into 20\% and 4\%.

$$
\begin{aligned}
& 10 \% \text { of } £ 300=£ 30 \text { so } 20 \%=£ 30 \times 2=£ 60 \\
& 1 \% \text { of } £ 300=£ 3 \text { so } 4 \%=£ 3 \times 4=£ 12
\end{aligned}
$$

$24 \%$ of $£ 300=£ 60+£ 12=£ 72$.
Therefore to increase $£ 300$ by $24 \%$, we now add $£ 72$ to the original amount. $£ 300+£ 72=£ 372$.

Decreasing by a percentage is the same process but subtracts rather than adds.

## Example 2: Percentage Change

You could be asked to calculate a change as a percentage. We use the following method:

$$
\% \text { Change }=\frac{\text { New Value }}{\text { Original Value }} \times 100
$$

Reminder: We always start with $100 \%$ of something, so if your percentage is over 100\%, subtract 100 from the percentage to find out by how much something has increased.

Example: A flat cost $£ 80,000$ last year and now costs $£ 108,000$. By what percentage has the value increased.
$\%$ Chane $=\frac{108,000}{80,000} \times 100=135 \%$

$$
\begin{aligned}
\text { Therefore } \% \text { increase } & =135 \%-100 \% \\
& =35 \%
\end{aligned}
$$

## Ratio 1



When quantities are to be mixed together, the ratio, or proportion of each quantity is often given. The ratio can be used to calculate the amount of each quantity, or to share a total into parts.

## Writing Ratios



In a bag of beads, there are 4 blue, 3 red, and 6 black beads.
The ratio of blue : red : black is $4: 3: 6$

## Simplifying Ratios

Ratios can be simplified in much the same way as fractions.

## Example 1

Purple paint can be made by mixing 10 tins of blue paint with 6 tins of red.
The ratio of blue to red can be written as 10:6

It can also be written as $5: 3$, as it is possible to split up the tins into 2 groups, each containing 5 tins of blue and 3 tins of red.


Blue : Red = $10: 6$
$=5: 3$

To simplify a ratio, divide each figure in the ratio by a common factor.

## Ratio 2

## Example 2

Simplify each ratio:
a) $4: 6$ $=2: 3$

Divide each figure by 2
b) $24: 36$
$=2: 3$
c) $6: 3: 12$ figure by 12

Divide each figure by 3

## Example 3

Concrete is made by mixing 20 kg of sand with 4 kg cement. Write the ratio of Sand: Cement in its simplest form.

$$
\text { Sand } \begin{aligned}
: \text { Cement } & =20: 4 \\
& =5: 1
\end{aligned}
$$

## Using Ratios

The ratio of fruit to nuts in a chocolate bar is 3 : 2. If a bar contains 15 g of fruit, what weight of nuts will it contain?


We try to figure out what have we multiplied 3 by to get to 15 ? 5 , hence why we multiply each side by 5 .

This means that the chocolate bar contains 10 g of nuts.

## Information Handling: Tables

It is sometimes useful to display information in graphs, charts or tables

Example The table below shows the average maximum temperatures (in degrees Celsius) in Barcelona and Edinburgh.

|  | J | F | M | A | M | J | J | A | S | $O$ | N | D |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Barcelona | 13 | 14 | 15 | 17 | 20 | 24 | 27 | 27 | 25 | 21 | 16 | 14 |
| Edinburgh | 6 | 6 | 8 | 11 | 14 | 17 | 18 | 18 | 16 | 13 | 8 | 6 |

The average temperature in June in Barcelona is $24^{\circ} \mathrm{C}$.

Frequency Tables are used to present information. Often data is grouped in intervals

Example 2 Homework marks for Class 4B.

| 27 | 30 | 23 | 24 | 22 | 35 | 24 | 33 | 38 | 43 | 18 | 29 | 28 | 28 | 27 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 33 | 36 | 30 | 43 | 50 | 30 | 25 | 26 | 37 | 35 | 20 | 22 | 24 | 31 | 48 |


| Mark | Tally | Frequency |
| :--- | :--- | :--- |
| $16-20$ | II | 2 |
| $21-25$ | HI II | 7 |
| $26-30$ | HI IIII | 9 |
| $31-35$ | HI | 5 |
| $36-40$ | III | 3 |
| $41-45$ | II | 2 |
| $46-50$ | II | 2 |

Each mark is recorded in the table by a tally mark. Tally marks are grouped in 5's to make it easier to read and count.

## Information Handling: Bar Graphs/ Historgrams



Bar graphs and Histograms are often used to display data. They must not be confused as being the same.
Bar Graphs are used to present discrete* or non numerical data*, whereas histograms are used to present continuous data*. (See key words for explanation of these terms)
All graphs should have a title, and each axis must be labelled.

Example 1 Example of a Bar Graph
How do pupils travel to school?


An even space should be between each bar and every bar should be of equal width. (Also leave a space between vertical axis and the first bar).

Example 2 Example of a histogram
The graph below shows the homework marks for Class 4B.


Important-there should be no space between each bar.

## Information Handling : Line Graphs



Line graphs consist of a series of points which are plotted, then joined by a line. The trend of a graph is a general description of it, usually looking from left to right.

Example 1 The graph below shows Heather's weight over 14 weeks as she follows an exercise programme.

Heather's weight


The trend of this graph is that her weight is decreasing.

Example 2 Graph of average temperatures in Edinburgh and Barcelona.


## Information Handling : Scatter Graphs

> A scatter diagram is used to display the relationship between two variables. A pattern may appear on the graph. This is called correlation.

Example The table below shows the height and arm apn of a group of first year boys. This is then plotted as a series of points on the graph below.

| Arm <br> Span <br> (cm) | 150 | 157 | 155 | 142 | 153 | 143 | 140 | 145 | 144 | 150 | 148 | 160 | 150 | 156 | 136 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Height <br> (cm) | 153 | 155 | 157 | 145 | 152 | 141 | 138 | 145 | 148 | 151 | 145 | 165 | 152 | 154 | 137 |



The graph shows a general trend, that as the arm span increases, so does height. This graph shows a positive correlation. (The points generally go upwards looking from left to right).

The straight line drawn is called the line of best fit. This line can be used to provide estimates. For example, a boy of arm span 150 cm would be expected to have a height of around 149 cm .
Note that in some subjects, it is a requirement that the axes start from 0.

## Information Handling: Pie Charts

A pie chart can be used to display information. Each sector (slice) of the chart represents a different category. The size of each category can be worked out as a fraction of the total using the number of divisions or by measuring angles.

Example $\quad 30$ pupils were asked the colour of their eyes. The results are shown in the pie chart below:


How many pupils had brown eyes?
The pie chart is divided up into ten parts, so the pupils with brown eyes represent $\frac{2}{10}$ of the total.
$\frac{2}{10}$ Of $30=6$, so 6 pupils had brown eyes.

If no divisions are marked, we can work out the fraction by measuring the angle of each sector.

The angle in the brown sector is $72^{\circ}$, so the number of pupils with brown eyes
$=\frac{72}{360} \times 30=6$ pupils.

If you find all of the values, you can check your answers! They should totals to 30!

## Information Handling : Averages

To provide information about a set of data, the average value may be given. There are 3 ways of finding the average valuethe mean, the median and the mode. It could also be useful to see how spread out the information is, for this we use the range.

## Mean

The mean is found by adding all the data together and dividing by the number of values given.

## Median

The median is the middle value when all the data is written in numerical order (if there are two middle values, the median is half-way between these values).

## Mode

The mode is the value that occurs most often.

## Range

The range of a set of data is a measure of spread.
Range $=$ Highest Value-Lowest Value.

Example Class 1A scored the following marks for their homework assignment. Find the mean, median, mode and range of the results.

$$
6,9.7,5,6,6,10,9,8,4,8,5,7
$$

Mean $=\underline{6+9+7+5+6+6+10+9+8+4+8+5+7}=\underline{90}=6.923 \ldots$

$$
13
$$13

Mean $=6.9$ to 1 decimal place .

Ordered values:

$$
\begin{gathered}
4,5,5,6,6,6,7,7,8,8,9,9,10 \\
\text { Median }=7
\end{gathered}
$$

6 is the most frequent mark, so Mode $=6$
Range $=10-4=6$

## Scientific Notation or Standard Form



In engineering and scientific calculations you often deal with very small or very large numbers, for example 0.000000345 or $870,000,000$. To avoid writing these very long numbers a system has been develped, known as scientific notation (standard form) which enables us to write numbers much more concisely.

The rules when writing a number in standard form is that first you write down a number between 1 and 10, then you write $\times 10$ (to the power of a number). In the Sciences the power of the number tends to be a multiple of 3 , in Maths the power can be any number.

## Example

Write 81900000000000 in standard form:
$81900000000000=8.19 \times 10^{13}$

It's $10^{13}$ because the digits have moved 13 places to the right to get to the number 8.19

## Example

Write 0.0000012 in standard form:
$0.0000012=1.2 \times 10^{-6}$
It's $10^{-6}$ because the digits have moved 6 places to the left to get to the number 1.2

On a calculator, you usually enter a number in standard form as follows: Type in the first number (the one between 1 and 10). Press EXP or $\times 10^{x}$. Type in the power to which 10 is risen.

Interesting facts
Mass of Earth $=5974200000000000000000000 \mathrm{~kg}=5.9742 \times 10^{24} \mathrm{~kg}$
Mass of an electron $=0.00000000000000000000000000000092 \mathrm{~kg}=9.2 \times 10^{-31} \mathrm{~kg}$

## Measurement



The common units used in Maths are:

## Length

Millimetres ( mm ), Centimetres ( cm ), Metres ( m ) and Kilometres (km)

## Area

Square Centimetres ( $\mathrm{cm}^{2}$ ), Square Metres $\left(\mathrm{m}^{2}\right)$, etc.

## Volume

Cubic Centimetres $\left(\mathrm{cm}^{3}\right)$, Cubic Metres $\left(\mathrm{m}^{3}\right)$, etc.

Important! Do NOT try to convert between units of area or volume, convert your length units first then calculate area or volume!

## Liquid Volume

Millilitres (ml), Litres (I)

## Weight

Grams (g), Kilograms (kg)


## Perimeter, Area and Volume

## Perimeter

The perimeter of a shape is the distance the whole way around a shape.

Example


## Area

The area of a 2D shape is "how much space it takes up". Individual shapes have individual formulae to calculate their areas. For each shape we substitute into the formula and can calculate the area from there. Units are always in square units.

$A=L^{2}$
rectangle

$A=L B$
$A=\frac{1}{2} B H$
TRIANGLE

$A=\pi r^{2}$

## Volume

The volume of a 3D shape is "how much space it takes up". Individual shapes have individual formulae to calculate their volume. For each shape we substitute into the formula and can calculate the volume from there. Units are always in cubed units.


> Volume of Cuboid $=$
> $=$ Length $\times$ Breadth $\times$ Height
> $=$ LBH

## Mathematical Literacy (Key Words):

| Add; Addition (+) | To combine 2 or more numbers to get one number (called the sum or the total) <br> Example: $12+76=88$ |
| :---: | :---: |
| a.m. | (ante meridiem) Any time in the morning (between midnight snd 12 noon). |
| Approximate | An estimated answer, often obtained by rounding to nearest 10 , 100 or decimal place. |
| Calculate | Find the answer to a problem. It doesn't mean that you must use a calculator! |
| Continuous Data | Has an infinite number of possible values within a selected range. They could get placed on a number line with no gaps (e.g. temperature, height, length) |
| Data | A collection of information (may include facts, numbers or measurements |
| Discrete | Can only have a finite or limited number of possible values. Shoe sizes are an example of discrete data because sizes 6 and 7 mean something, but 6.3 for example does not. |
| Denominator | The bottom number in a fraction (the number of parts into which the whole is split). |
| Difference (-) | The amount between two numbers (subtraction). Example: The difference between 50 and 36 is 14 $50-36=14$ |
| Division ( - ) | Sharing a number into equal parts $24 \div 6=4$ |
| Double | Multiply by 2 |
| Equals (=) | Makes or has the same amount as. |
| Equivalent fractions | Fractions which have the same value. Example $\frac{6}{12}$ and $\frac{1}{2}$ are equivalent fractions. |
| Estimate | To make an approximate or rough answer, often by rounding. |
| Evaluate | To work out the answer. |


| Even | A number that is divisible by 2. <br> Even numbers end with $0,2,4,6$ or 8. |
| :---: | :---: |
| Factor | A number which divides exactly into another number, leaving no remainder. <br> Example: The factors of 15 are $1,3,5,15$. |
| Frequency | How often something happens. In a set of data, the number of times a number or category occurs. |
| Greater than (>) | Is bigger or more than. <br> Example: 10 is greater than 6. $10>6$ |
| Least | The lowest number in a group (minimum). |
| Less than (<) | Is smaller or lower than. <br> Example: 15 is less than $21.15<21$. |
| Maximum | The largest or highest number in a group |
| Mean | The arithmetic average of a set of numbers-See Page 25 |
| Median | Another type of average-the middle number of an ordered set of data-See page 25 |
| Minus (-) | To subtract. |
| Mode | Another type of average-the most frequent number or category (See page 25) |
| Most | The largest or highest number in a group (maximum). |
| Multiple | A number which can be divided by a particular number, leaving no remainder. <br> Example: Some of the multiples of 4 are $4,8,12,16 \ldots$ |
| Multiply (x) | To combine an amount a particular number of times. Example $6 \times 4=24$ |
| Negative Number | A number less than zero. Shown by a minus sign. Example: -5 is a negative number |
| Numerator | The top number of a fraction |
| Non Numerical Data | Data which is non numerical eg favourite football team, favourite sweet etc. Can be put into a category |
| Odd number | A number which is not divisible by 2 . Odd numbers end in $1,3,5$, 7 or 9. |


| Operations | The four basic operations are addition, subtraction, <br> multiplication and division. |
| :--- | :--- |
| Order of <br> operations | The order in which operations should be done. (BODMAS/ <br> BIDMAS - See page ). |
| Place Value | The value of a digit dependent on it's place in the number <br> Example: in the number 1573.4, the 5 has a place value of 100 |
| p.m. | (post meridiem) Any time in the afternoon or evening (Between <br> 12 noon and midnight) |
| Prime Number | A number that has exactly 2 factors (can only be divided by 1 <br> and itself). Note 1 is not a prime number as it only has 1 factor. |
| Product | The answer when two numbers are multiplied together. <br> Example: The product of 5 and 4 is 20. |
| Range | How spread out your data is, calculated by Highest Value - <br> Lowest Value. |
| Remainder | The amount left over when dividing a number. |
| Share | To divide into equal groups |
| Substitute | To replace one thing with another. Commonly used when using a <br> formula. |
| Sum | The total of a group of numbers (found by adding). |
| Total | The sum of a group of numbers (found by adding). |

